

## Pattern Matching

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## Outline and Reading

- ◆ Strings (§9.1.1)
- ◆ Pattern matching algorithms
  - Brute-force algorithm (§9.1.2)
  - Boyer-Moore algorithm (§9.1.3)
  - Knuth-Morris-Pratt algorithm (§9.1.4)

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## Strings

- ◆ A string is a sequence of characters
- ◆ Examples of strings:
  - Java program
  - HTML document
  - DNA sequence
  - Digitized image
- ◆ An alphabet  $\Sigma$  is the set of possible characters for a family of strings
- ◆ Example of alphabets:
  - ASCII
  - Unicode
  - $\{0, 1\}$
  - $\{A, C, G, T\}$
- ◆ Let  $P$  be a string of size  $m$ 
  - A substring  $P[i..j]$  of  $P$  is the subsequence of  $P$  consisting of the characters with ranks between  $i$  and  $j$
  - A prefix of  $P$  is a substring of the type  $P[0..i]$
  - A suffix of  $P$  is a substring of the type  $P[i..m-1]$
- ◆ Given strings  $T$  (text) and  $P$  (pattern), the pattern matching problem consists of finding a substring of  $T$  equal to  $P$
- ◆ Applications:
  - Text editors
  - Search engines
  - Biological research

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## Brute-Force Algorithm

- ◆ The brute-force pattern matching algorithm compares the pattern  $P$  with the text  $T$  for each possible shift of  $P$  relative to  $T$ , until either
  - a match is found, or
  - all placements of the pattern have been tried
- ◆ Brute-force pattern matching runs in time  $O(nm)$
- ◆ Example of worst case:
  - $T = aaa \dots ah$
  - $P = aaah$
  - may occur in images and DNA sequences
  - unlikely in English text

**Algorithm *BruteForceMatch(T, P)***

**Input** text  $T$  of size  $n$  and pattern  $P$  of size  $m$

**Output** starting index of a substring of  $T$  equal to  $P$  or  $-1$  if no such substring exists

```

for  $i \leftarrow 0$  to  $n - m$ 
  { test shift  $i$  of the pattern }
   $j \leftarrow 0$ 
  while  $j < m \wedge T[i+j] = P[j]$ 
     $j \leftarrow j + 1$ 
  if  $j = m$ 
    return  $i$  { match at  $i$  }
else
  return  $-1$  { no match }
```

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## Boyer-Moore's Algorithm (1)

- ◆ The Boyer-Moore's pattern matching algorithm is based on two heuristics
- Looking-glass heuristic:** Compare  $P$  with a subsequence of  $T$  moving backwards
- Character-jump heuristic:** When a mismatch occurs at  $T[i] = c$ 
  - If  $P$  contains  $c$ , shift  $P$  to align the last occurrence of  $c$  in  $P$  with  $T[i]$
  - Else, shift  $P$  to align  $P[0]$  with  $T[i+1]$
- ◆ Example

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## Last-Occurrence Function

- ◆ Boyer-Moore's algorithm preprocesses the pattern  $P$  and the alphabet  $\Sigma$  to build the last-occurrence function  $L$  mapping  $\Sigma$  to integers, where  $L(c)$  is defined as
  - the largest index  $i$  such that  $P[i] = c$  or
  - $-1$  if no such index exists
- ◆ Example:
 

$c$	$a$	$b$	$c$	$d$
$L(c)$	4	5	3	-1

  - $\Sigma = \{a, b, c, d\}$
  - $P = abacab$
- ◆ The last-occurrence function can be represented by an array indexed by the numeric codes of the characters
- ◆ The last-occurrence function can be computed in time  $O(m+s)$ , where  $m$  is the size of  $P$  and  $s$  is the size of  $\Sigma$

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